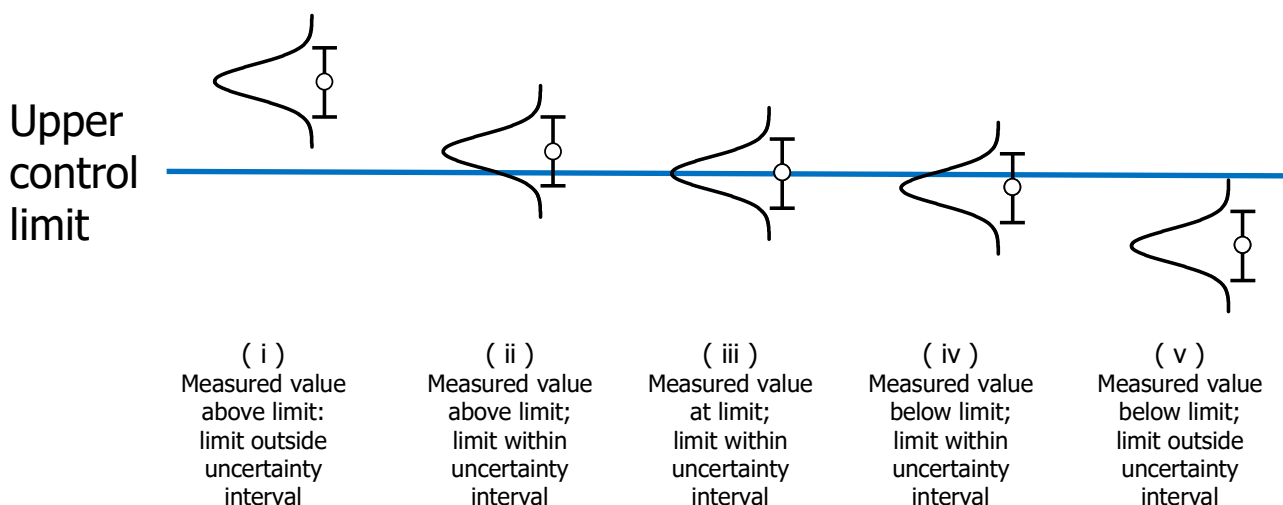


Use of uncertainty in compliance

In this leaflet we present the Eurachem/CITAC guide on how to assess compliance with a specification or a regulation

Introduction

When test results are used to assess compliance, i.e. to decide whether specifications or regulations are met, the measurement uncertainty of the test results has to be taken into account. Assessment of compliance for cases **i** and **v** in the Figure below is clear – the measurement results including the uncertainty interval are clearly above or below the limit value. In the other cases the decision is not clear since the uncertainty interval overlaps the limit value. The Eurachem/CITAC guide [1] gives guidance on cases **ii**, **iii** and **iv**.



We need acceptance & rejection zones

In order to judge whether the results in cases **ii**, **iii**, and **iv** comply with the limit value we need a decision rule, based on the risks associated with making a wrong decision. This decision rule enables a guard band, g , to be calculated which defines an acceptance zone and a rejection zone. If the measurement value is within the acceptance zone the specifications are met and we can conclude compliance. If the measured value is in the rejection zone, we can conclude non-compliance. The intersection between these two zones is called the decision limit. A guard band is normally chosen so that for a measured value in the acceptance zone the probability of correct acceptance is more than or equal to a defined confidence value α . Note that a guard band, $g = 0$ can also be used. This is called *simple acceptance*.

Decision rule

A decision rule should have a well-documented method of determining the location of acceptance and rejection zones, ideally including acceptable levels of probability, P , that the value of the measurand 1) lies within the specification limit, *high confidence of correct acceptance* (low probability of false acceptance) or 2) lies outside the specification limit, *high confidence of correct rejection* (low probability of false rejection).

Information needed for assessing compliance

The following information is needed:

- measurand clearly specified;
- specification stating upper or lower limit or both;
- decision rule;
- measured value;
- measurement uncertainty for a measured value at the limit(s).

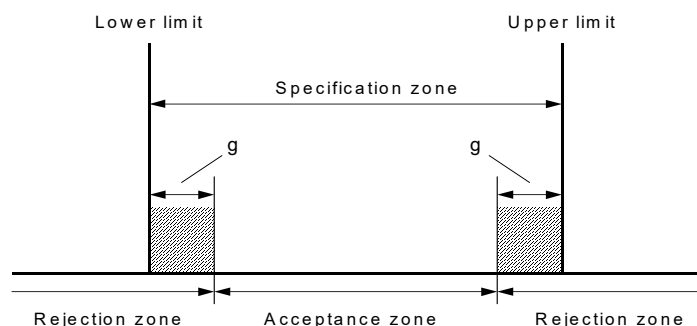


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Example focusing on correct acceptance

Measurand	Mass fraction of nickel, Ni in a batch of steel delivered to a customer.
Uncertainty	$U = 0.2\%$ Ni, $k = 2$ (95 %). Standard uncertainty, $u = 0.1\%$ Ni. This uncertainty includes both sampling uncertainty for the batch and analytical uncertainty.
Specification	The specification zone is from the lower limit 16.0 % Ni to the upper limit 18.0 % Ni.
Decision rule <i>High confidence of correct acceptance</i>	<i>The acceptance range is the mass fraction where it can be decided with a confidence level of approximately 95 % ($\alpha = 0.05$) that the batch has a mass fraction above the lower limit and below the upper limit.</i>
Guard band	Each guard band is calculated as $1.64u \approx 0.17\%$ (rounded upward for safety) with k value 1.64 from the one-tailed upper 95 % quantile of the normal distribution.
Acceptance zone	16.2 % Ni to 17.8 % Ni, after rounding to one decimal place.
Measured value	16.1 % Ni



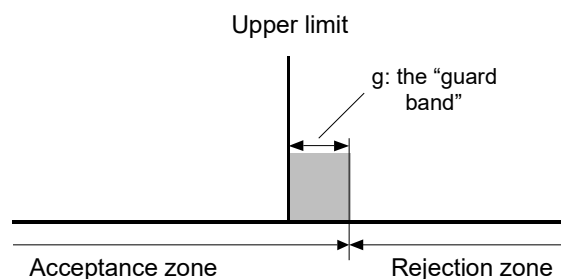
Guard bands (g), and acceptance and a rejection zones based on a lower and upper limit and a decision rule stating high confidence of correct acceptance

The measured value, 16.1 % Ni, is below the lower acceptance limit of 16.2 %; that is, in the rejection zone. The batch is non-compliant. Note – if the decision rule stated *simple acceptance* the acceptance zone would be 16.0 % to 18.0 % and the batch would be compliant.

Example focusing on correct rejection

Measurand	Mass fraction of a banned substance in a sample.
Uncertainty	The relative standard uncertainty u_{rel} is 35 %.
Specification	Upper limit is 2 ng/g.
Decision rule <i>High confidence of correct rejection</i>	<i>The concentration of the banned substance will be deemed to be above the limit if the probability of the value of the concentration being greater than the limit is 95 % or greater.</i>
Guard band	The guard band g for <i>correct rejection</i> is 1.6 ng/g assuming a lognormal distribution (due to the high relative uncertainty – see further Guide Annex A, Case 4 [1]).
Acceptance limit	3.6 ng/g
Measured value	3.3 ng/g

The measured value, 3.3 ng/g, is below the acceptance limit of 3.6 ng/g; that is, in the acceptance zone. The sample is compliant. Note that the assumption of the type of distribution is crucial. If assuming a normal distribution in this case the acceptance limit would be 3.2 ng/g and the sample would not be compliant.



Guard band (g), and acceptance and a rejection zones based on a decision rule stating high confidence of correct rejection

More information / further reading

[1] A. Williams and B. Magnusson (eds.) Eurachem/CITAC Guide: Use of uncertainty information in compliance assessment (2nd ed. 2021). Available from www.eurachem.org.